

**References on Multilevel Modeling**  
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Below we have listed a number of references to books, chapters, and articles that we have found useful in our own research and teaching. Within each topic references are listed alphabetically. Note that the references provided under each topic are not exhaustive and are intended merely to provide an entrance point to the literature; the inclusion or exclusion of any given paper is not intended to represent endorsement or lack thereof of the paper. Finally, we have generally avoided listing more technical work.

**General Books**

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**General Articles**

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### **Substantive Examples Using Multilevel Models**

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